On the Effects of Droplet Loading on the Structure of Spray Jets

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Abstract

This paper uses advanced laser diagnostics to investigate the effects of droplet loading on the structure and mixing patterns of sprays in a non-reacting, turbulent jet. A nozzle designed at University of Sydney with the objective of studying spray flames has been used for producing a two phase flow in a co-flowing air stream with well defined boundary conditions. Varying the quantity of liquid injective will vary the number density of the droplets in the flow.

The co-flowing air stream is seeded with a fixed concentration of nitric oxide, NO which will act as a conserved scalar. Laser induced fluorescence of NO is exploited to provide a direct quantitative measure of the mixture fraction. Radial profiles of the mean and the rms of mixture fraction has been collected at various axial positions in jets with different spray loadings. It is found that mixture fraction profiles are different from those measured in turbulent gaseous jets and increasing the droplet loading increases the mixture fraction of the jet due to evaporating droplets.

Introduction

Spray flows are common in many industrial applications ranging from chemical processing to burners, gas turbine combustors and internal combustion engines. The physics and chemistry of spray flows in these applications are made complex by the unknown interactions between the droplets, the turbulence, mixing and chemical processes. Accurate models are needed to study these phenomena’s and improve future designs of these spray systems. Due to scarcity of detailed experimental data that isolate each of the complex features of a spray, which include droplet size, velocity, evaporation, droplet interaction with gas flow, turbulence, mixing and chemical reaction, has made it difficult to validate such models. Faeth, [1, 2] has reviewed previous work on spray combustion and has listed a number of databases for flows involving sprays.

The spray combustion project at the University of Sydney is dedicated to developing an improved understanding of spray jets and flames and to developing a comprehensive database in a laboratory burner that is experimentally tractable as well as numerically simple enough to isolate effects of turbulence, evaporation, droplet interactions, and chemical reactions. Previous papers by Chen et al, [3-6] provide initial data for sparsely loaded spray jets, where fine sprays created by air blast generated droplets in a glass nebuliser. The Sauter mean diameter ranges from 14 to 35 microns. Starmer et al., [7] then measured droplet size and velocity in a sparsely loaded piloted spray flame, where the droplets in the spray was created using a ultrasonic nebuliser, which is more akin to sprays seen in industrial applications.

This paper is the continuation of the on going work to study the mixing behaviour of a spray loaded turbulent jet. As reported previously a technique has been developed [8] to measure vapour phase mixture fraction in a spray jet. Nitric oxide, NO is seeded in the coflow shrouding the jet. Mass fraction of NO is used as a conserved scalar, $Z_i$ in determining the mixture fraction, $\xi$

$$\xi_{cflow} = \frac{Z_1 - Z_{i,2}}{Z_{i,1} - Z_{i,2}}$$

where subscripts 1 and 2 denote the fuel and oxidiser streams [9].

The mixture fraction of the jet stream is then given by $1-\xi_{cflow}$.

Mixed induced fluorescence of NO has been used extensively in many single-point and imaging applications. Barlow et al [10, 11] have measured nascent NO at single points in turbulent flames while Laurendeau’s group has seeded NO in premixed flames of varying stoichiometries and studied its interaction with the flows. The objective of these studies and others [12-17] was to develop the LIF-NO technique as temperature diagnostic tools using the ratio of one or more NO fluorescence lines. For the present study, LIF signal from NO is used for determining the mass fraction of NO and thus the mixture fraction in a turbulent jet loaded with spray droplets. The excitation line used is the $Q_1+P_2(14.5)$ transition of the A-X(0,0) band at 226.03 nm.

Mixing fields in axisymmetric gaseous jets have been studied by many researchers. Antonia et al, [18] has studied heated round gaseous jets, provided the mixing fields using temperature as the conserved scalar. Pitts [19, 20] and Mi et al [21] have carried out extensive work on axisymmetric jets, the former studying the effects of global density ratio and Reynolds number on the centreline mixing behaviour and the later studying mixing characteristics of jets from contoured nozzle, an orifice and a pipe. Measurements in sprays jets are compared to those obtained earlier for gaseous jets to highlight the effects of sprays on the mixing structure.

Experimental Setup

The schematic diagram of the experimental setup is given in [8]. Excitation wavelength for NO LIF is generated by employing the second harmonic ($\lambda = 532$nm) of a Quanta-Ray Pro-Series Pulsed Nd:YAG laser to pump a Sirah dye Laser , which provides visible radiation at 622.18nm. The dye laser fundamental is sum frequency mixed with the frequency tripled Nd:YAG laser beam (355nm) to obtain UV light at 226.03nm. The excited beam was spatially separated from the residual beams using Pellin-Broca prisms. The laser energy was 9.3ml/pulse. The laser beam was focussed into a sheet of thickness 200 microns using a 400 mm focal length cylindrical lens. The fluorescence signal corresponding to the $\gamma(0,1)$ band of NO was collected on an intensified flow master CCD camera. The signal was filtered using a short wave pass dichroic filter transmitting light at 236nm with a bandwidth of 10nm. A custom made filter made by BARR Associates was used for filtering strong Mie signal from the droplets. This long pass filter had a optical density of over 5 at 226nm and 59% transmittance at 236 nm. The object size of the raw images is 32x25 mm. The images
are taken at a range of axial positions ranging from \( x/D = 0 \) to \( x/D = 20 \). A second Flow Master camera is used for monitoring the laser energy on a shot to shot basis.

**Spray Burner**

A 3D schematic of the burner setup is shown in figure 1a. The burner nozzle and coflow assembly is mounted inside a 29 x 29 cm vertical wind tunnel. The outlet of the wind tunnel has screens mounted on it to smooth out the flow. The inside diameter of the coflow is 104 mm. In unconfined flows, air would be entrained from the surrounding into the co-flowing stream hence reducing the region where the initial boundary conditions prevail. Moreover, the entrained air is not seeded with NO hence un-validating its use as a conserved scalar. To prevent this, shrouds are added to isolate the seeded co-flow from the surrounding up to the measurement location. These co-flow shroud extensions are used for \( x/D \) equals 5, 10, 15 and 20, where \( x \) is the axial distance from the jet exit plane. The lengths of these extensions from the jet and coflow exit planes are 32.5, 72.5, 123.5 and 174.5 mm for the respective \( x/D \) positions. At \( x/D = 0 \) the jet and the coflow have the same exit plane as shown in figure 1b. Meshed wire screens are used in the coflow to smooth out the flow and give a top hat velocity profile at the exit plane. The diameter of the jet is 10.5 mm.

**Initial Conditions**

The bulk velocity of the coflow, pilot and the wind tunnel is 3 m/s. Nitric oxide, NO is seeded at 200ppm in the coflow and pilot streams. Table 1 gives a summary of the four cases studied here. The first case is an air jet, where L stands for low jet carrier velocity and A for Air without spray. Cases LL, LM and LH are the 3 air jets with spray, where the second letters L, M and H denotes droplet loading of low, medium and high. Ultrasonically generated droplets with near zero momentum are entrained in the carrier stream. The droplet loading is varied by varying the mass flow rate of the liquid acetone. Flow rates were measured using rotameters, tri-flats and Tylan electronic mass flow meters.

<table>
<thead>
<tr>
<th>Case</th>
<th>Air volume flowrate l/min</th>
<th>Acetone mass flowrate kg/min</th>
</tr>
</thead>
<tbody>
<tr>
<td>LA</td>
<td>114.3</td>
<td>0</td>
</tr>
<tr>
<td>LL</td>
<td>114.3</td>
<td>0.024</td>
</tr>
<tr>
<td>LM</td>
<td>114.3</td>
<td>0.045</td>
</tr>
<tr>
<td>LH</td>
<td>114.3</td>
<td>0.075</td>
</tr>
</tbody>
</table>

Table 1. Air and fuel flow rates for 1 air and 3 spray jet cases.

**Air Jet Flow Simulation**

The commercially available computational fluid dynamics package Fluent is used to perform computations of simple gaseous jets that are used as a baseline for comparison with measurements. Fluent is widely used and has therefore undergone extensive testing making it particularly useful for this type of simulations. The computation domain size is 300 mm x 145 mm. The coflow wall had an extension of length 275 mm similar to the experiment. A staggered grid with 73000 cells is used for the computation. All calculations are solved assuming steady flow. The model used is axisymmetric standard \( k-\varepsilon \). Dally et al. [22] has shown that the \( k-\varepsilon \) model over predicts the decay rate and the spreading rate for a round jet. Dally concluded that using \( C_{\varepsilon 1} = 1.6 \) gave a better representation of the decay and spreading rate for a round jet. Therefore constants \( C_{\varepsilon 1} \) and \( C_{\varepsilon 2} \) used are 1.6 and 2.02.

Argon has been used as a marker of mixture fraction in the calculation of an air jet issuing in air co-flow. Argon, at 200ppm is seeded in the coflow and pilot to simulate Case LA. A no slip boundary condition has been used for the walls of the jet, pilot, coflow, and the wind tunnel. The boundary conditions are given in table 2. The solution converged after 2300 iterations.

<table>
<thead>
<tr>
<th>Jet Inlet Mass flow rate kg/s</th>
<th>0.0024799</th>
</tr>
</thead>
<tbody>
<tr>
<td>Turbulent intensity %</td>
<td>14</td>
</tr>
<tr>
<td>Pilot Inlet Velocity m/s</td>
<td>3</td>
</tr>
<tr>
<td>Turbulent intensity %</td>
<td>3</td>
</tr>
<tr>
<td>Coflow Inlet Velocity m/s</td>
<td>3</td>
</tr>
<tr>
<td>Turbulent intensity %</td>
<td>3</td>
</tr>
<tr>
<td>Wind Tunnel Inlet Velocity m/s</td>
<td>3</td>
</tr>
<tr>
<td>Turbulent intensity %</td>
<td>3</td>
</tr>
</tbody>
</table>

Table 2. Boundary condition for Case LA for Fluent simulation.
Results

Validation with Air Jet

The validity of the NO LIF technique is confirmed first by comparing the measurements made in gaseous jets with other experiments made in similar flows as well as with calculations. Case LA is used here as a baseline and Fig. 2 shows the centreline axial decay of mean mixture fraction for the current measurements compared with two other data sets reported in the literature. Antonia, [18] and Mi, [21] have shown an $x^{-1}$ dependence of mean centreline mixture fraction. The current experiment data shows a similar dependence. The axial decay of mixture fraction for Case LA from the Fluent simulation also follows a similar trend. The simulations also show a $1/x$ dependence of mean mixture fraction.

![Figure 2](image2.png)

Figure 2. Mean centreline decay of mixture fraction in a axisymmetric air jet. Both experiment and simulation show similar trends that $\xi_{CL}(x) \sim (1/x)$.

Comparison of the radial profiles of the mean mixture fraction at $x/D = 0.5, 5, 10, 15$ and $20$ between current experiment and the simulations is shown in figure 3. The simulation is predicting slightly faster spreading rate compared to the experiment for $x/D$ 5 and 10. This could be due to the value of the constants for generation $C_{11}$, and destruction $C_{22}$, of the turbulent dissipation term used for these calculations. For $x/D = 15$ and 20 the radial profiles from the experiment and the simulation look much closer.

![Figure 3](image3.png)

Figure 3. Comparison between radial distributions of mean mixture fraction for the air jet case LA, measured using the NO LIF technique and calculated via Fluent simulations.
Mixture Fraction Fields in Spray Jets

Figure 5 and 6 show 2D instantaneous field of mixture fraction for cases LA LL LM and LH at five axial stations. The individual image size is 32 mm x 10 mm. At the jet exit plane the mixture fraction is unity as shown by the images. There are small rolling eddies forming at the edge of the jet which entrains air from the pilot and coflow streams. The bulk jet velocity is constant and hence the structure of the rolling eddies at x/D = 0 for all the cases are similar. Few droplets are visible for cases LL LM and LH at the exit plane too.

As the jet spreads larger eddies are visible further downstream. These eddies increase the entrainment of coflowing air, which then reduces mixture fraction in the air jet, LA but increases the evaporation of the spray droplets in the spray jets LL, LM and LH and thus giving higher mixture fraction. The high mixture fraction is due to the increase in vapour concentration which slows down the diffusion of coflow air into the core of the jet. There are air pockets that get entrained in the jet and some move to the centre of the jet. Droplets can be seen at downstream locations. The images also show that the spray loaded jets have a larger spread rate compared to the air jet. This could be due to the existence of droplets.

The higher spreading rate of the spray loaded jets can be confirmed by the radial profiles of mean mixture fraction plotted in figure 7. At x/D = 0.5 and 5 there is no difference in the radial profiles of mean mixture fraction for the 4 cases except the centreline values. A small increase is observed in mixture fraction for cases LL, LM and LH at x/D = 10, with case LL showing the largest change. This could be due to low droplet number density and thus higher evaporation rate. At x/D = 15 and 20 the mixture fraction of the LH and LM cases increase with LH being the higher one. The radial profiles show that the air case LA has the lowest mixture fraction and it increases with the droplet loading.

The mean centreline decay of mixture fraction, $\xi_{CL}$, for the spray cases LL, LM and LH are compared with the air case LA in figure 4. The profiles of $\xi_{CL}$ for cases LL LM and LH increase as x/D increases. For x/D = 0.5 and 5, $\xi_{CL}$ for case LA is higher. At x/D = 10 all 4 case have almost similar $\xi_{CL}$ values. A distinct difference in $\xi_{CL}$ can be seen at x/D = 15 and 20. The LH case has a higher mixture fraction value at x/D = 15 compared to LL, LM and LA and as the x/D increases to 20 all 4 cases separate to show the effect of droplet loading on the mean mixture fraction. The increase in mixture fraction of the spray case is due to evaporation of spray droplets. As the droplet loading is increased the mixture fraction also increases.

Radial profiles of the rms fluctuations of mixture fraction, $\xi'$ are shown in figure 8 for five axial locations in the jets. At the jet exit plane all the profiles show similar trends with peak fluctuations at the edge. A transition can be seen on the jet centre line going from x/D = 0.5 to x/D = 20 where case LA and LL have higher $\xi'$ at lower x/D and case LM and LH has higher $\xi'$ at x/D greater than 10. At the edge of the jet at x/D = 20, case LM and LH, are showing large fluctuations of mixture fraction when compared with case LA. It is also interesting to note from the profiles shown here that the droplets generate turbulence as evident from the higher peaks obtained in $\xi'$ for the cases with increasing droplet loadings.

Acknowledgments

This work is supported by a grant from the Australian Research Council.

Conclusions

This study has shown that the NO LIF technique used in this paper to determine the mixture fraction of the vapour phase in a spray loaded jet is a valid technique. The data presented is a major step forward in creating a database for modellers to model a simple axisymmetric jet loaded with spray droplets. This study has provided profiles of mean and rms of mixture fraction in spray jets with varying droplet loading. It has been shown that increasing the droplet loading increases the mixture fraction. The increase in mixture fraction in a spray jet is due to evaporation of spray droplets. The turbulent fluctuation also increased as the droplet loading was increased. The evaporation rate could not be determined due to the unavailability of droplet and velocity data.

Future work on this project aims to study the interactions between the turbulence, droplet and mixture fraction fields. This requires carrying out additional measurements of droplet size distribution and velocity and turbulence field. Using these measurements combined with those presented here for mixture fraction, the evaporation rates may be extracted. Such estimates would be extremely useful for validating the sub-models currently used for the droplet evaporation rates.

Acknowledgments

This work is supported by a grant from the Australian Research Council.
Figure 5. 2D Instantaneous image of mixture fraction for case LA, LL, LM and LH at axial positions of x/D = 0.5, 5, 10, 15 and 20.
Figure 6. 2D Instantaneous image of mixture fraction for case LA LL LM and LH at axial positions of x/D = 0.5, 5, 10, 15 and 20.
Figure 7. Radial profiles of mean mixture fraction for cases LL, LM, LH, and LA at axial position of 0.5, 5, 10, 15 and 20.

Figure 8. Radial profiles of mixture fraction rms for cases LL, LM, LH, and LA at axial position of 0.5, 5, 10, 15 and 20.
References


Droplets Transport in a Microfluidic Chip for In Vitro Compartmentalisation

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Abstract

In vitro compartmentalisation is an emerging technology for protein evolution and selection. In this presentation, we will report the development of a microdrop-based microfluidic platform for in vitro enzyme evolution and selection applications. A microfluidic chip has been developed and fabricated using the standard photolithography method in conjunction with electroplating and hot embossing techniques. A cross channel geometry was used to focus liquid flows for droplet generation. To realize on-chip compartmentalised bio-reactions, two droplet generators were fabricated on the same chip. Experiments have been carried out to measure droplet size, generation rate and speed using a photographic technique. Droplet size was found to be decreasing with increasing focusing oil flow rate for a given aqueous phase flow rate. When two droplet generators are used in the same chip, the droplets may be generated asynchronously due to different flow conditions. If the droplets were significantly smaller than channel size, the faster moving droplets could pass the slower moving droplets with little coalescence. If the droplets were of the channel size, the faster moving droplets would break or fuse with the slow droplets. To achieve high rate of droplet fusion, active control should be in place for synchronous generation and fusion.

Introduction

In vitro compartmentalisation (IVC) refers to cell-like compartments generated artificially as reaction chambers. In biology, cells use walls to confine networks of chemical reactions so that these reactions can not be messed up or easily disturbed by the outside world. This organisational model inspired Tawfik and Griffiths (1998[13]) to develop a system using micron-size water droplets dispersed in oil medium in which individual gene sequences could be contained with the enzyme variant they encode. The emulsion droplets in IVC can have a size ranging from a few microns to a few hundreds microns. The potential high capacity (more than 10¹⁰ droplets per millilitre of sample) and ease of formation render it an ideal means of compartmentalising biochemical and genetic assays (Griffiths and Tawfik 2006[5]). Such a capacity can not be achieved in in conventional assays (a 10 µl assay in a 1536-well microtitre plate).

Although the IVC technology has only been developed recently, it has attracted a great deal of attention since the last few years. A number of review articles have been published such as Griffiths and Tawfik[4], Amstuts et al. [1], Leamon et al. [8], Rothe et al.[11], Kelly et al.[7]. Recently, there has been a number of studies on the development of lab-on-a-chip technologies for IVC applications (e.g. Link et al.[9], Hubeber et al.[6]). Drop generation using microfluidics has proven to be more advantageous than conventional lab methods since it can produce monodisperse droplets with controllable sizes. In addition, microfluidic technologies can also provide means of droplet splitting, fusion, sorting and in-drop detection.

The Synthetic Enzymes initiative in CSIRO is a multi-institutional effort aiming to develop enzymes with dramatically shifted functions or mechanisms that are capable of catalysing novel reactions not known in nature. This will be achieved by developing technology to introduce novel chemical groups to enzymes to synthesise enzymes using highly controllable cell-free methods, and to evolve enzymes using IVC technology. This paper will report some of the results in the IVC chip development. In particular, we will present some of the data on behaviour of droplets transport in microchannels.

Chip design and fabrication

The two commonly used methods for on-chip drop generation include a T-junction channel network (e.g. Nisisako et al.[10]) and a cross-junction (e.g. Anna et al.[12]). In the latter case, the flow is focused by the two side channels to form droplets. This method was used in the present study. A picture of the microchip is shown in Figure 1.

Figure 1: A picture of the fabricated droplet chip. The channel width is 115 µm at the nozzle and 207 µm at the main section.

The microchip was fabricated in a polycarbonate slide with dimensions of 75mm × 75mm and a thickness of 2mm. The microchip was fabricated in the CSIRO Microfabrication Laboratory, Clayton, VIC 3169, Australia. The microfluidic channel pattern was designed using a commercial layout tool and fabricated as a film mask. The mask pattern was exposed into a 70 µm layer of Laminar 5083 resist/stainless steel plate using a collimated UV exposure system. The exposed pattern was developed in a Na₂CO₃ solution and the resulting profile was replicated as a nickel shim by a two-stage process. Firstly, a thin layer of nickel was sputter deposited onto the patterned surface followed by a thicker electropolished layer (100 µm) in a nickel sulphamate bath. The nickel shim was subsequently used as a die to hot emboss the pattern of channels into polycarbonate chips. The embossing was performed in a planar hydraulic press at a temperature of 155°C. During embossing, the pressure was maintained for two minutes and then released after cooling to 50°C. The access holes were then drilled through the backside of the polycarbonate plate. Before laminating the capping layer, the polycarbonate chip was treated with oxygen plasma for 15 minutes. To access the microchannels in the chip, a nano-ports assembly was carefully glued to each liquid port.
Experimental Details
The droplet experiments were carried out in the CSIRO Microfluidics Laboratory at Highett, Melbourne, Australia. To produce water-in-oil droplets, the water solution was pumped from the left-hand side of the horizontal channel (Figure 2) while the oil solution was pumped simultaneously from the two inlets in the side channels.

![Figure 2: A sketch of drop formation principle.](image)

The symmetric oil branches and the water branch intersected at the inlet of the production channel which was directed towards downstream processing or waste. Droplets were formed when the aqueous jet breaks due to the shear force by the oil streams. The oil and water channels each had a width section of 315 μm which decreased to 115 μm at the junction point. The production channel had a width of 207 μm and all channels had the same depth of 70 μm. The cross section of each channel was rectangular. In the present study, deionised water was used for the aqueous phase while ETA oil was used as the organic phase. The ETA vegetable oil was manufactured by Goodman Fielder Food Services Limited, Australia. The kinematic viscosity of the aqueous phase while ETA oil was used as the organic phase. The ETA vegetable oil was manufactured by Goodman Fielder Food Services Limited, Australia. The kinematic viscosity of 1 mPaS. The interfacial tension between the walls and the oil phase has been reported as 0.033 N/m. Both the water and oil streams were generated by the use of two identical Razel A-99 syringe-pumps equipped with Terumo syringes of 5 ml capacity. The syringes were fitted with high grade filters in order to eliminate any potential microscopic contaminant in each of the phases. Droplet formation at the junction point was monitored visually by a Nikon Eclipse TE2000-U microscope and a video camera Basler A 6021C-2 equipped with a Nikon C-0.45× demagnification lens. The camera was capable of capturing images at a frequency of 30 frames per second. The experimental setup is shown in Figure 3.

![Figure 3: Experimental set-up for droplet generation and control. The droplet chip was placed in a chip holder with liquid and electrical interface for liquid and electrical current deliveries.](image)

The analysis of the images has shown that the average droplet size, \(d\), decreased monotonically with increasing oil flow rate \(Q_o\) as seen in Figure 5. From the study by GI Taylor[14], the drop formation is a result of the shearing force applied by the oil streams on the water stream at the junction. The predicted droplet size \(d\) is proportional to \(\sigma / \mu \gamma\), where \(\sigma\) is the interfacial tension, \(\mu\) is the continuous phase viscosity and \(\gamma\) is the shear rate. For a nozzle size of \(D\) and a flow rate of the continuous phase \(Q_o\), \(\gamma\) is proportional to \(Q_o / D^3\). Therefore the drop size should depend on the flow rate inversely (e.g. Cristini and Tan[3]), via,

\[
d \propto \frac{\sigma D^3}{\mu Q_o}.
\]  

Results
Drop generation by flow focusing
In Figure 4, a series of sample images show a typical decrease of water droplet size when the flow rate of the continuous oil stream was increased. The two oil streams which intersected laterally acted to shear off the water jet formed at the entrance of the junction. With increase in flow rate of the oil, it can be seen from the images that the water jet tip became sharper and very fine droplets could be regularly generated.

![Figure 4: Visualization of the droplet generation in the microfluidic chip under different flow conditions. The water flow rate \(Q_w\) was 0.031 ml/h. The main channel had a width of 207μm and a height of 70μm. The oil flow rates were 0.096, 0.287, 0.446 and 0.955 ml/h for cases (a) to (d), respectively.](image)

The interfacial tension between the walls and the oil phase was lower than that between the walls and the dispersed water phase, stable water-in-oil (W/O) droplets could be formed in the current conditions. Initially the channels were completely filled with the oil phase using the lowest flow rate before commencement of the water stream. The flow rate in the water stream was gradually increased until the observation of droplets. The lowest flow rates at which droplet could be generated were 0.031 ml/h and 0.095 ml/h for the water phase and oil phase, respectively. The effect of the continuous flow rate on the droplet size was then investigated by increasing the oil flow rate gradually. A sequence of pictures captured from the video camera was saved to a computer for each oil flow rate in order to process digitally the images. The droplet size was measured by image processing of the recorded frame. The size of droplets was averaged over a batch of consecutive images captured for specific water and oil flow rates. The water flow rate was fixed to 0.031 ml/h and the oil flow rate was increased from 0.095 ml/h to 0.955 ml/h.

\[d \propto \frac{\sigma D^3}{\mu Q_o}\]  

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