## Chapter 5: Simple Modelling

Where we examine various modelling abilities of CLP languages



2

## Modelling

- Choose the variables that will be used to represent the parameters of the problem (this may be straightforward or difficult)
- Model the idealized relationships between these variables using the primitive constraints available in the domain

3







Modelling Choice Multiple rules allow modelling relationships that involve choice • E.g. tables of data using multiple facts. father(jim,edward). mother(maggy,fi). father(jim,maggy). mother(fi,lillian). father(edward,peter). father(edward,helen). father(edward,kitty). father(bill,fi). 7



```
For the set of t
```





$$if 0 \le S \le E/100$$

$$call_payoff(S,C,E) = \begin{cases} -C & \text{if } 0 \le S \le E/100 \\ 100S - E - C & \text{if } S \ge E/100 \end{cases}$$
Model a function with *n* arguments as a predicate with *n*+1 arguments. Tests are constraints, and result is an equation.
$$buy_call_payoff(S,C,E,P) := 0 \le S, S \le E/100, P = -C.$$

$$buy_call_payoff(S,C,E,P) := 0 \le S \le E/100, P = 100*S - E - C.$$

```
Add an extra argument B=1 (buy), B = -1 (sell)
call_option(B,S,C,E,P) :-
    0 <= S, S <= E/100, P = -C * B.
call_option(B,S,C,E,P) :-
    S >= E/100, P = (100*S - E - C)*B.
The goal (the original call option question)
call_option(1, 7, 200, 300, P)
has answer P = 200
```

butterfly(S, P1 + 2\*P2 + P3) :-  
Buy = 1, Sell = -1,  
call\_option(Buy, S, 100, 500, P1),  
put\_option(Sell, S, 200, 300, P2),  
call\_option(Buy, S, 400, 100, P3).  
Defines the relationship in previous graph  
P >= 0, butterfly(S,P).  
has two answers  

$$P = 100S - 200 \land 2 \le S \land S \le 3$$
  
 $P = -100S + 400 \land 3 \le S \land S \le 4$  <sup>14</sup>













```
Security Translation Example

Pseudo C code for the mortgage problem

float mg2(float P, int T, float I, float R)
{
    if (T >= 1) {
        P = P + P * I - R;
        T = T - 1;
        return mg2(P, T, I, R); }
    else
        return P;
}
Make each variable only take one value
```



```
Security Translation Example

Pseudo C code for the mortgage problem

mg4(float P,int T,float I,float R,float *B)
{
    if (T >= 1) {
        NP = P + P * I - R;
        NT = T - 1;
        mg4(NP, NT, I, R, B); }
    else
        *B = P;
}
Replace tests and assignments by constraints
```



![](_page_12_Figure_1.jpeg)

![](_page_12_Figure_2.jpeg)

```
f(X,Y) := X = 1.
p(X,Y) := Y = 1.
p(X,Y) := Y = 1.
x = 0, Y = 0, \text{ minimize}(p(X,Y), X+Y)
Answers: X = 1 \land Y = 0 and X = 0 \land Y = 1

x = 0, X = Y, \text{ minimize}(true, X-Y)
Answer: X = 0 \land X = Y

minimize(butterfly(S,P), -P)

Answer: S = 3 \land P = 100
```

![](_page_13_Figure_2.jpeg)

![](_page_14_Figure_1.jpeg)

![](_page_14_Figure_2.jpeg)

![](_page_15_Figure_1.jpeg)