An investigation of channel flow with a smooth air–water interface

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Abstract Experiments and numerical simulation are used to investigate fully developed laminar and turbulent channel flow with an air–water interface as the lower boundary condition. Laser Doppler velocimetry measurements of streamwise and wall-normal velocity components are made over a range of Reynolds number based upon channel height and bulk velocity from 1100 to 4300, which encompasses the laminar, transitional and low Reynolds numbers turbulent regimes. The results show that the airflow statistics near the stationary wall are not significantly altered by the air–water moving interface and reflect those found in channel flows. The mean statistics on the water interface side largely exhibit results similar to simulated Poiseuille–Couette flow (PCF) with a solid moving wall. For second-order statistics, however, the simulation and experimental results show some discrepancies near the moving water surface, suggesting that a full two-phase simulation is required. A momentum and energy transport tubes analysis is investigated for laminar and turbulent PCFs. This analysis builds upon the classical notion of a streamtube and indicates that part of the energy from the pressure gradient is transported towards the stationary wall and is dissipated as heat inside the energy tubes, while the remainder is transmitted to the moving wall. For the experiments, the airflow energy is transmitted towards the water to overcome the drag force and drive the water forward; therefore, the amount of energy transferred to the water is higher than the energy transferred to a solid moving wall.

1 Introduction

Numerous engineering applications involve an interaction between a gas flowing adjacent to a moving liquid. This interaction has been investigated extensively due to its application in the petroleum, chemical and nuclear industries as well as in geophysical and environmental sciences (Banerjee 2007). Despite the efforts in this area of research, there remains an incomplete understanding of turbulent gas motion near a liquid interface. This arises from difficulties in experimentally measuring or numerically simulating velocity fields in the vicinity of moving surfaces and is further complicated by the turbulent nature of the flow in most applications of practical interest. The investigation of this flow (concurrent gas–liquid flow) is considerably complicated by the two-phase boundary condition. In this study, we test how well a simplified Poiseuille–Couette flow can be used to act as a proxy for the real two-phase flow, and in doing so, clarify aspects of the underlying physics.

A number of experimental studies have looked at the interaction between a turbulent airflow and a water film flowing parallel to it. Only a few, however, have looked at the present configuration, which is an air–water channel. Hanratty and Engen (1957) conducted experiments in such a channel to examine the interaction between a turbulent air stream above a moving water film. Their results indicated no distortion in the airflow velocity profile for a smooth water surface and for a water surface with ripples. Hanratty and Engen (1957) and Dykhno et al. (1994)
measured the air velocity profiles and found that the maximal velocity shifts 10–12% towards the stationary wall. These trends display a significantly different behaviour with those observed by later researchers. For example, both Paras et al. (1998) and Wongwises and Kalinitchenko (2002) measured the air velocity profiles and found that the maximal velocity shifts towards the interface. The inconclusive results of this basic statistical quantity suggest that further study is warranted.

The objective of this research is to determine the effects of an air–water interaction on the airflow statistics near the interface and stationary wall in a (nominally) fully developed channel flow. The streamwise and wall-normal velocity components are obtained using two-component laser Doppler velocimetry (LDV). A surrogate direct numerical simulation (DNS) of a Poiseuille–Couette flow is also performed using the experimentally obtained interface velocity as the boundary condition at $\delta^{+} = 135$, where $\delta$ is the half channel height, $U_\tau$ is the friction velocity, and $\nu$ is the kinematic viscosity. This allows one to comment on the accuracy of a reduced simulation, which is a substantially cheaper computation to perform in comparison with a two-phase simulation. These comparisons also provide insights into the underlying flow physics. The flow physics of the two-phase flow and PCF is further clarified using a momentum and energy transport tube analysis. Meyers and Meneveau (2013) describe the properties of momentum and energy transport tubes, which are analogous to a streamtube.

2 Experimental details

2.1 Experimental facility

The experiments were conducted in the facility schematically shown in Fig. 1. The air height, $H$, is 24.9 mm with an aspect ratio of 11. The depth of the water beneath the air flow was 350 mm. The aspect ratio is sufficient to ensure a nominally two-dimensional flow (Dean 1978). Air is drawn through the diffuser using a suction fan. Water circulation was nominally promoted by a fixed speed pump in the direction of airflow. The pump alone produces a surface velocity of approximately 0.02 m/s. The concurrent flow in combination with a weir generates a stable moving air–water interface that was primarily driven by the airflow itself. Water enters the tank from a 32-mm-diameter PVC pipe that is split using two 80-mm-diameter pipes. The water then passes through two mesh screens and a honeycomb section to ensure water flow uniformity at the channel inlet. The surface velocity of the water flow was quantified using a video camera to track insoluble Polyethylene particles floating on the surface (specific gravity of 0.95–0.96). Also, it was observed that the pump (without running the fan) produces a water surface oscillation of less than ±0.15 mm (0.5% $H$) and equates to 0.5–1.5 viscous units.

2.2 LDV measurements

The LDV system was calibrated using two methods: a spinning disc (Park et al. 2002) and a spinning wire (Bean and Hall 1999; Kurihara et al. 2002). The preferred method of calibration for a two-component LDV system is a spinning disc. The measurement volume is focused onto the surface of a roughened disc that is driven by a servomotor. The horizontal ($U$) and vertical ($V$) components of velocity were calibrated by positioning the measurement volume at $90^\circ$ and $0^\circ$, respectively. The total uncertainty in both components was approximately 0.5%. A spinning wire was used to ensure that the LDV system sampling rate of each channel is correct. A significant difference between the spinning wire and disc methods is that only a single particle (e.g. wire tip) passes through the probe volume per revolution in comparison with multiple particles. The nominal standard deviation in the sampling rate over a range in angular velocity from 300 to 600 RPM for the $U$ and $V$ components is 0.0016 and 0.0019 1/s, respectively.

The LDV measurement volume had dimensions of 0.085 mm in height, 0.085 mm in width and 1.2 mm in length for the blue beam (488.0 nm), and 0.089 mm in height, 0.089 mm in width and 1.3 mm in length for the green beam (514.5 nm) (Kurihara et al. 2002). The
measurement volume in terms of viscous units was $\Delta^+ \simeq 7$, $\Delta^+ \simeq 0.5$, and $\Delta^+ \simeq 0.5$ at $\delta^+ = 131$. Further details regarding the LDV measurement volume, calibration methods, and results can be found in Madad (2013).

### 2.3 Inner normalization and scaling

Scaling analysis of turbulence quantities requires an estimate of the wall shear stress, $\tau_{sw}$. The friction velocity is derived from the wall shear stress, $U_f = \sqrt{\tau_w/\rho}$, where $\rho$ is the fluid density. For fully developed, two-dimensional Poiseuille–Couette flow, use of the mean statement of momentum conservation yields,

$$\tau_{mw} - \tau_{sw} = H \frac{dp}{dx} \quad (1)$$

where $\tau_{sw} = \mu \frac{du}{dy} \big|_{sw}$ and $\tau_{mw} = \mu \frac{du}{dy} \big|_{mw}$ are the wall shear stress at the moving wall and stationary wall, respectively, $\mu$ is the dynamic viscosity, $p$ is the mean pressure, and $x$ is the streamwise axis. The contribution from the vertical sidewalls contributes to the overall pressure drop in Eq. 1, but is negligible since the aspect ratio is greater than 10. The friction velocity for the stationary wall, $U_{frw}$, and moving wall, $U_{fwmw}$, are determined using a four-point linear curve-fit of $U$ within the linear sublayer. The uncertainty in the balance between the left-hand side and right-hand side of Eq. 1 is less than 7 %.

Telbany and Reynolds (1980) suggested the moving wall velocity scaling is likely to be proportional to $(y/H)^{0.5}$ and $y^{-1}$, where $\gamma$ is the ratio of the Couette ($HU_{sw}/\nu$) to Poiseuille ($HU_b/\nu$) flow Reynolds number, $U_b$ is the bulk velocity, and $y$ is the distance from the moving wall. In this study, the following relationship proposed by Thurlow and Klewicki (2000) is applied to obtain the local friction velocity of the moving wall

$$U_{fwmw} = \frac{U_{fwmw}}{1 - 5y \sqrt{y/H}} \quad (2)$$

Using $U_{fwmw}$ improves the collapse of the data in comparison with $U_{frw}$. Note that for the present analysis, this only changes $U_{fwmw}$ on average by 4.6 %.

### 2.4 Experimental parameters

The experimental data were measured at a fixed downstream distance of 170H from the inlet. This distance exceeds that required for fully developed flow (130H) (Lien et al. 2004; Monty 2004) for the case of solid wall channels. In the present case, the airflow can be considered streamwise homogeneous to a very good approximation. Since the LDV settings are the same for all the measurements, the spatial resolution degrades slightly with increasing $\delta^+$. For parameter range and symbol definition, see Table 1. The lowest Reynolds number, $Re = HU_b/\nu = 1170 (\delta^+ = 40.4)$, is in the laminar regime and the remainder are in the transitionally turbulent regime with a smooth moving water surface. The highest Reynolds number, $Re = 4267 (\delta^+ = 140)$, corresponds to the first appearance of ripples on the water surface.

<table>
<thead>
<tr>
<th>$Re$</th>
<th>$\delta^+_{sw}$</th>
<th>$\delta^+_{mw}$</th>
<th>$U_{fsw}$ (m/s)</th>
<th>$U_{fwmw}$ (m/s)</th>
<th>Symbol</th>
</tr>
</thead>
<tbody>
<tr>
<td>1170</td>
<td>40.4</td>
<td>40.4</td>
<td>0.051</td>
<td>0.050</td>
<td>$\times$</td>
</tr>
<tr>
<td>2237</td>
<td>76.0</td>
<td>75.1</td>
<td>0.087</td>
<td>0.086</td>
<td>$\checkmark$</td>
</tr>
<tr>
<td>2581</td>
<td>86.9</td>
<td>84.0</td>
<td>0.101</td>
<td>0.098</td>
<td>$+$</td>
</tr>
<tr>
<td>2958</td>
<td>101</td>
<td>98.7</td>
<td>0.102</td>
<td>0.100</td>
<td>$\circ$</td>
</tr>
<tr>
<td>3683</td>
<td>118</td>
<td>113</td>
<td>0.129</td>
<td>0.123</td>
<td>$&lt;$</td>
</tr>
<tr>
<td>3710</td>
<td>125</td>
<td>118</td>
<td>0.142</td>
<td>0.134</td>
<td>$\square$</td>
</tr>
<tr>
<td>3836</td>
<td>131</td>
<td>124</td>
<td>0.144</td>
<td>0.139</td>
<td>$\circ$</td>
</tr>
<tr>
<td>4003</td>
<td>135</td>
<td>132</td>
<td>0.146</td>
<td>0.142</td>
<td>$\triangle$</td>
</tr>
<tr>
<td>4267</td>
<td>144</td>
<td>138</td>
<td>0.167</td>
<td>0.160</td>
<td>$\ast$</td>
</tr>
</tbody>
</table>

Note that the subscript $sw$ and $mw$ denote stationary and moving wall, respectively.

The direct numerical simulation of Poiseuille–Couette flow is based upon a spectral element/ Fourier spatial discretization with a second-order velocity-correction projection scheme for the temporal discretization as described by Blackburn and Sherwin (2004). The Fourier coordinate requires geometric homogeneity in the spanwise direction, while the remaining planar geometry is discretized using nodal spectral elements with a Gauss–Lobatto–Legendre local mesh in each element. A tenth order Legendre polynomial is employed within each spectral element. The computational domain length is sufficient for the convergence of the statistics considered in this work according to Chin et al. (2010). For this simulation, the time-step is $\Delta t = 0.001$ (dimensionless) and the collection of statistics is initiated after sufficient time (a minimum of five wash-through times based on the bulk flow speed and domain length) has elapsed to allow the flow to reach a statistically steady state. The
turbulence statistics are then averaged over 20 wash-through times to achieve convergence. The simulation parameters are: \( \Delta x^+ = 9.94, \Delta y_{wall}^+ = 0.075, \Delta y_{centre}^+ = 3.15, \) and \( \Delta z^+ = 4.97. \) The fully developed turbulent PCF simulation is conducted at a Reynolds number of \( \delta^+ = 135. \) The fixed velocity of the moving water surface obtained from the experimental results is used as the boundary condition. At \( \delta^+ = 135, \) the velocity at the air–water interface is \( U_{mw} = 0.12 \text{ m/s}. \)

3 Results

3.1 Mean velocity profiles

The mean velocity profiles normalized by the maximum velocity, \( U_m, \) over the Reynolds number range of \( 40 < \delta^+ < 145 \) are presented in Fig. 2a. The analytical solution for laminar Poiseuille–Couette flow is in agreement with the measured data at \( \delta^+ = 40. \) As expected, the experimental data show that the mean velocity profiles flatten in the non-laminar regime. A comparison of the experimental mean velocity profile at \( \delta^+ = 135 \) and simulated PCF is shown in Fig. 2b. The simulation data match the experimental data near the stationary wall \( (0 < y/H < 0.12) \) and reasonably well over the remainder of the channel height.

3.2 Skin friction

The coefficient of friction, \( C_f, \) for pure Poiseuille flows is obtained using Dean’s equation (Dean 1978) and is given as

\[
C_f = 0.073 \Re^{-0.25}
\] (3)

The \( C_f \) values obtained from Eq. 3 and the experimental data for the stationary wall/moving wall surface are shown in Fig. 3. Very good agreement is seen between the stationary wall friction coefficients and the results of Dean’s empirical equation. As expected from PCF with a forward moving wall, e.g. (Thurlow and Klewicki 2000), the values of \( C_f \) for the moving side are lower than the stationary side; here, \( C_{f_{mw}} \) is on average about 5% lower than \( C_{f_{sw}}. \)

3.3 Inner-normalized mean velocity profiles

The inner-normalized mean velocity profiles for the stationary side and the moving side (using \( U_{\tau_{sw}} \) and \( U_{\tau_{mw}}, \) respectively) are shown in Fig. 4a, b, respectively. For the moving side, the water surface velocity is subtracted from the mean velocities. These profiles merge onto a single curve for \( y^+ \leq 20 \) and collapse well on
the $U^+ = y^+$ curve within the viscous sublayer (Fig. 4). Beyond $y^+ = 30$, the higher Reynolds number profiles approach a logarithmic-like dependence. These trends are similar to the results of Elsnab et al. (2011) for post-laminar channel flows over a range of low Reynolds numbers.

Comparisons between the inner-normalized velocity profiles from the experiment and simulated PCF for the stationary and moving side are shown in Fig. 5a, b, respectively, as well as DNS channel flow data by Laadhari (2002) provided that the wall velocity is subtracted from the moving wall data.

The root-mean-square (rms) streamwise velocity fluctuations, $u_{\text{rms}}$, for the stationary side is presented in Fig. 6a. The peak position in $u_{\text{rms}}$ for all experimental results is located at $y^+ \approx 15$, and the maximum value is on average about 5% lower than DNS profiles of Tsukahara et al. (2005) at $\delta^+ = 80$ and 110. The $u_{\text{rms}}$ for the moving side is shown in Fig. 6b. The position of the peak $u_{\text{rms}}$ for the water side is $y^+ \approx 17$, and the maximum value is about 4% lower than for the present stationary wall data (see Fig. 8a). These results are in good agreement with the observations of Thurlow and Klewicki (2000) and Spencer et al. (2009).

The rms wall-normal velocity fluctuations, $v_{\text{rms}}$, for the stationary wall along with channel flow DNS results by Tsukahara et al. (2005) at $\delta^+ = 80$ and 110 are shown in Fig. 7a, and for the moving side in Fig. 7b. The variation in $v_{\text{rms}}$ from the stationary wall ($y/H = 0$) towards the moving water surface is shown in Fig. 8b. The peak wall-normal turbulence intensity near the air–water interface

3.4 Turbulent velocity fluctuations

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At higher Reynolds numbers, $124 \leq \delta^+ \leq 144$, is higher than near the stationary wall ($y/H = 0$). However, this is not the case for lower Reynolds numbers, $76 \leq \delta^+ \leq 118$. For $76 \leq \delta^+ \leq 118$, the maximum value of $v_{\text{rms}}$ remains the same near the stationary and moving surfaces and shows similar behaviour to Poiseuille flow. For $124 \leq \delta^+ \leq 144$, the maximum value near the stationary wall is lower than the interface value. The effect of the moving water on $v_{\text{rms}}$ does not agree with PCF studies and becomes more significant with increasing Reynolds number. A possible explanation for this observation is the physical difference between a solid moving wall and an air–water interface (presence of water surface oscillation). Because the air–water interface is compliant and not shear-free, the parallel surface fluctuations are not zero due to the slip boundary condition, as they are for a solid surface. Additionally, because the interface is compliant and only kept flat by surface tension, the normal fluctuations can be larger near the interface. This, of course, depends on the relative strength of the interface stresses as compared to the turbulent pressure fluctuations.

The streamwise rms velocity fluctuation profiles of the simulated PCF and current experiment at $\delta^+ = 135$ are essentially identical for the stationary side, with the peak near the stationary wall located at $y^+ = 14$ and 16 for the simulation and experiment, respectively. Close to the moving water surface, however, the peak appears farther from the moving wall for the experiment ($y^+ = 20$) than for the simulation ($y^+ = 15$). The peak of $v_{\text{rms}}$ near the stationary wall is higher than the peak near the moving wall for the simulation, while the opposite occurs for the experiment at $\delta^+ = 135$. The overall features of the experimentally derived rms profiles and their differences with the simulation are clarified in Fig. 8a, b.

### 3.5 Reynolds stress

The inner-normalized Reynolds stress profiles for both stationary wall and moving water side are shown in Fig. 9. The Reynolds stress increases in peak value and the shifts outward in viscous units with increasing Reynolds number for both the stationary and moving water side of the channel. The Reynolds stress varies linearly from the peak towards...
the centreline for the stationary side and is nearly linear for
the moving water side. This linear variation is consistent
with channel flow results, which can be derived from clas-
sical analysis of the once-integrated mean momentum equa-
tion. For the moving side, the experimental data at
$\delta^+ = 135$ show much higher Reynolds stress from the core region to
the buffer layer (corresponding to $0.5 < y/H < 0.9$) com-
pared to simulated PCF. Water level oscillations may at least
partly underlie this rather dramatic difference.

### 3.6 Turbulence kinetic energy production

The turbulent kinetic energy production, $E_p^+(y) = - < uv >^+ \frac{\partial U^+}{\partial y^+}$, is a dominant term in the kinetic
energy budget. Profiles of $E_p^+$ normalized by the station-
ary wall friction velocity for the experiment and simula-
tion are shown in Fig. 10. Both profiles exhibit consistent
results with diminishing energy production close to the
channel centreline and peaks near both walls with amplifi-
cation of $E_p^+$ near the stationary wall and attenuation near

the moving wall. Spencer et al. (2009) also observed a
similar trend, as the energy production is lower close to
the co-moving wall.
It is also of interest to consider the difference between the energy production profiles of experimental and simulated results for half of the channel towards the moving wall \((0.5 < y/H < 1)\). Although the peak near the moving wall (DNS) is higher than the peak near the moving water surface (experiment), the area under both profiles is approximately the same, and the net energy production of the DNS is about 5 \% larger than the experiment, which is attributed to the difference in \(<uv>^+\) velocities since the mean velocity gradient is essentially symmetric across the channel.

### 3.7 Transport of momentum and energy

Momentum and energy transport can be graphically depicted using transport tube analyses, which builds upon the classical notion of a streamtube. Meyers and Meneveau (2013) used these concepts to visualize turbulent flow processes associated with wind turbine arrays. There is no exchange of momentum or energy through the corresponding tube mantle. Momentum and energy transport tubes, like streamtubes, are not Galilean invariant. The similarity between classical streamtubes and the momentum/energy transport tubes is that the flux is constant across sections except for integral effects of sinks and sources due to viscous dissipation and turbulent kinetic energy production. For steady, inviscid flow, streamtubes, momentum and energy transport tubes all coincide since the viscous and Reynolds stress are zero. However, for turbulent flows, momentum tubes can be significantly different from the energy transport tubes due to the Reynolds stresses. The combination of laminar Couette and Poiseuille flows is of interest because its structure provides a basis for better understanding of momentum and energy transport in the presence of a no-slip and a moving wall. The velocity profile for laminar PCF is \(U = (dp/dx)(y^2 - yH)/(2\mu) + yU_{mw}/H\). Using the velocity profile, the two components of momentum flux are

\[
\mathcal{F}_1 = U^2 = \left( \frac{dp}{dx} \frac{y(y - 1)}{2\mu} + yU_{mw} \right)^2 \tag{4}
\]

\[
\mathcal{F}_2 = -v \frac{\partial U}{\partial y} = -v \left( \frac{1}{2\mu} \frac{dp}{dx} (2y - 1) + U_{mw} \right) \tag{5}
\]

where it is assumed \(H = 1\). Integration of \(dy/dx = \mathcal{F}_2/\mathcal{F}_1\) and rearrangement allows the momentum lines, \(x = y(x)\), to be written as

\[
x = \frac{C}{8v} y^4 + \frac{C - U_{mw}}{4v} y^3 - \frac{(C - U_{mw})^2}{16v} y^2 - \frac{(C - U_{mw})^3}{16C^2v} y - \frac{(C - U_{mw})^4}{32C^3v} \ln(U_{mw} - C + 2Cy) \tag{6}
\]

where \(C = (dp/dx)/(2\mu)\).

The momentum transfer lines for different moving wall velocities are constructed using Eq. 6. The velocity profiles and corresponding momentum lines for different PCFs normalized with the moving wall velocity for a constant pressure gradient are shown in Fig. 11. The evolution of the momentum transport lines from “Poiseuille-type flow” (a) to “Couette-type flow” (d) is shown in these figures. The momentum added in the bulk flow through the pressure gradient is transported towards the sidewalls because the pressure gradient dominates. However, the location of the zero momentum transport line, \(Y_{ZCM=0}\), continually moves towards the moving wall with increasing wall velocity. At the zero momentum transport line, the total advection of momentum occurs horizontally. By increasing the moving wall velocity, the effect of Couette flow dominates over the pressure gradient and the momentum lines eventually form a profile similar to pure Couette flow.

The energy transport lines for laminar flow have similar shape as the momentum lines, but twice the slope. The interpretation for energy tubes for Poiseuille- and Couette-type flows is as follows: for Poiseuille-type flow (Fig. 11a), the kinetic energy of the pressure gradient is dissipated as heat inside the tubes towards the stationary wall (top wall) and transferred to the moving wall (bottom wall). By increasing the moving wall speed, a larger part of the energy from the pressure gradient is transferred to the moving wall and converted to the work done by the moving wall. The rest of the energy is dissipated as heat inside the mantle and is directed towards the stationary wall (see Fig. 11b, c). For the Couette-type flow (Fig. 11d), the work done by the moving wall dominates over the pressure gradient, and the energy of moving wall is transferred entirely towards the stationary wall. This energy is dissipated as heat inside the energy tubes before reaching the stationary wall.

The momentum lines for the laminar airflow PCF solution and the laminar experimental data are shown in Fig. 12. The momentum lines for the analytical and experimental results are similar, although the location of the zero momentum transport line from the experimental data moves slightly towards the moving water \((y \approx 0.47H)\), in comparison with the analytical solution \((y \approx 0.5H)\).

As indicated with arrows in Fig. 12, the momentum added to the bulk flow through the pressure gradient is transferred towards the stationary top wall and the moving water surface (bottom wall). The effect of the pressure gradient dominates over the effect of the moving wall (Couette effect), and the momentum lines of the current experiment are similar to the laminar pure Poiseuille flow. However, the location of the zero momentum transport line for the experimental results moves slightly towards the moving water surface. The momentum added by the pressure...
Fig. 11  Velocity profiles and momentum lines of laminar PCF with different moving wall velocity (a through d corresponds to the different velocity profiles shown at the left). The dashed-line is the zero momentum transport line. $y = 1$ is the stationary wall. Note that it is assumed $H = 1$. 
gradient to the airflow is transmitted to the water, which in turn drives the water forward. The momentum from the moving water surface is then transported towards the stationary bottom wall of the water tank over a large streamwise distance \((110H)\).

### 3.7.1 Turbulent flow

Using the results presented in Meyers and Meneveau (2013), the two components of the energy flux for the turbulent airflow are formed as follows:

\[
\mathbf{F}_1 = \frac{U^3}{2} + U < uu >
\]

\[
\mathbf{F}_2 = U \left( < uv > - \nu \frac{\partial U}{\partial y} \right)
\]

Hence, the slopes of the tangent lines of this vector field are given by:

\[
\frac{dy}{dx} = \frac{\mathbf{F}_2}{\mathbf{F}_1} = \frac{< uv > - \nu \frac{\partial U}{\partial y}}{\frac{U^3}{2} + < uu >}
\]

Numerical integration yields an energy line for turbulent airflow with one stationary wall and a moving water surface. The energy lines of the experiment and simulation are shown in Fig. 13. The data in this figure reveal that the energy line of the simulated Poiseuille–Couette flow with a moving solid wall for this Reynolds number is similar to pure Poiseuille flow since the ratio of Couette to Poiseuille Reynolds number is low \((\gamma = 0.07)\). In addition, the location of the zero energy transport line (no vertical transport) is at the channel’s centreline. However, the energy line of the current experiment shows its location moves significantly towards the moving wall \((y/H \approx 0.3)\). Near both the stationary and the moving wall, the transport lines become vertical as more of the energy transport occurs through viscous diffusion. Close to the stationary wall, this vertical energy line is about \(0.05H\) from the wall. Both the DNS and experimental data show the same trend. The simulated PCF data show that near the moving wall the vertical line extends the same distance into the flow. In contrast, the experimental data show that this line extends much farther \((0.2H)\) from the moving water surface.

![Fig. 12](image1.png) The momentum lines of the laminar airflow. Analytical solution for laminar PCF (a) and experimental data of the airflow with a moving water surface (b), where \(y/H = 1\) is the stationary wall.

![Fig. 13](image2.png) Energy lines of airflow for simulated data (a) and experimental data (b) where \(y/H = 1\) is the stationary wall.
4 Concluding remarks

The results show that over the range of Reynolds numbers investigated, the airflow statistics near the stationary wall are not affected by the air–water moving interface and are comparable with pure Poiseuille flows. Also, a number of the statistics on the moving side show results similar to the simulated PCF with a solid moving wall. It can be concluded that, in order to simulate airflow within a fixed wall and a moving water with a smooth surface (no waves), there is minimal need to simulate water flow underneath the interface to obtain nominally accurate mean airflow statistics at a fixed streamwise distance, i.e. a moving water surface can be simulated as a solid moving wall. However, for second-order statistics, a two-phase simulation (from bottom wall of the water tank to top wall of the air channel) is required, as simulation and experimental results have discrepancies near the moving water surface. Here, momentum and energy tube analysis reveals that these discrepancies are due to a greater consumption of the airflow energy to overcome the water drag and drive the water forward, as compared to the PCF configuration with a moving solid wall.

Despite these differences in momentum and energy at the surface, an interesting question remains as to why the mean statistics for the two-phase flow still agree reasonably well with the PCF case. Here we speculate that surface tension may spatially localize the effect of the boundary condition. Essentially, the water surface behaves like an elastic sheet due to force from surface tension. The ratio of the viscous to surface tension forces is the capillary number (Ca). At \( \delta^+ = 135 \), it is estimated that \( Ca < 0.1 \) (characteristic length is the fully developed length of the flow - 2.44 m), therefore, surface tension forces are greater than viscous forces acting on the water surface. When surface tension dominates, a good approximation for the mean flow is obtained by modelling the two-phase flow as PCF. As \( \delta^+ \) increases, ripples form on the water surface indicating the gravity effects become important, i.e. \( U/U_b = f(Re,Ca,Fr) \), where \( Fr \) is the Froude number. Clearly this becomes an increasingly complicated flow that requires further investigation.

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