

# Flow Characteristics of the Outer Part of a Circular Jet with and Without Excitation

A.J. CHAMBERS

Senior Lecturer in Mechanical Engineering, The University of Newcastle

R.A. ANTONIA

Professor of Mechanical Engineering, The University of Newcastle

and

A.K.M.F. HUSSAIN

Professor of Mechanical Engineering, University of Houston, Texas, USA

**SUMMARY** Statistics of flow reversal in the outer region of the near field of a circular jet are examined with and without acoustic excitation. These statistics, which include the mean duration and frequency of flow reversal, are obtained with a hot-wire/cold-wire arrangement, designed so that the cold wire senses the thermal wake of the hot-wire. The organisational influence of excitation on the large structure is largest near the nozzle but weakens with distance downstream. At ten diameters from the nozzle, the velocity structure parameters of the turbulence are unaffected by the excitation.

## 1 INTRODUCTION

It seems well established that the organised large structures in the near field of a jet plays an important role in the dynamics of the flow and in particular in mixing and in sound generation. Controlled excitation of the jet can accentuate the characteristics of these structures and provide a relatively simple means of studying them. Hussain & Zaman (1979) carried out a detailed exploration of vortex pairing in the near field of an acoustically excited circular jet (exhausting into still air) by applying phase averaging techniques. An inevitable difficulty encountered in this type of study is that the flow on the low-speed side of the mixing layer undergoes reversal. At some phases during the passage of the vortices, instantaneous measurements, by a directionally insensitive hot-wire, of the velocity vector direction and the vorticity are consequently in error. In a previous paper (Antonia et al, 1980) we investigated errors, due to flow reversal, in simultaneous measurements of temperature and velocity in the far field, of a circular jet. The experimental technique used to identify and obtain statistical information of the reverse flow regions is applied here to the near field of a circular jet, with and without excitation. The intention, in this paper, is not to attempt to correct velocity and other statistics influenced by the flow reversal but simply to ascertain the influence of excitation on the large structure through the statistics of the flow reversal regions.

## 2 EXPERIMENTAL ARRANGEMENT

The jet facility used in this study is described by Hussain & Zedan (1978). The nozzle (diameter  $D = 7.62$  cm) had a cubic profile (Hussain & Ramjee, 1976) and was made from laminated wood blocks so that the jet emerged through a 30 cm dia. end plate. The exit Reynolds number  $R_D = DU_j/\nu$  was  $1.1 \times 10^5$ . For the unexcited jet, the exit turbulence intensity at the centreline was about 0.3%. With excitation, the Strouhal number,  $St = fD/U_j$  was 0.37 and the exit turbulence intensity was 3%. The exit boundary layer mean profile agreed with the Blasius profile.

The measurements presented here were made with a hot-cold wire arrangement with the wires orthogonal and normal to the axial flow direction. The cold wire was approximately 1 mm upstream of the hot wire and was used to detect flow reversals by sensing the hot wire wake. The hot wire, 5  $\mu$ m dia. (Pt-10% Rh) was

operated by a DISA55M10 constant temperature anemometer at an overheat of 0.8. The cold wire, 0.6  $\mu$ m dia. (Pt-10% Rh), was operated by a constant current bridge, the value of the current being set at 0.1 mA. Signals from the linearised constant temperature anemometer and from the constant current bridge were recorded, following suitable signal conditioning, on a Hewlett-Packard FM3960A tape recorder. The analogue tapes were later played back and digitized on a DEC PDP 11/20 computer (sample rate  $\approx 1000$  Hz, record duration  $\approx 50$  s), for further data processing.

Measurements of flow velocity and flow reversals were made at  $x/D = 2, 3, 6$  and 10 in the outer part ( $r/r_{1/2} > 1.0$ ) of the jet. Here,  $r$  is the radial distance from the jet centreline and  $r_{1/2}$  is the jet half radius.

## 3 RESULTS AND DISCUSSION

Figure 1 shows that mean axial velocity profiles at different  $x$  are essentially unaffected by the excitation. For  $x/D > 3$ , the profiles are in reasonable agreement with Chevray & Tutu's (1978) measurements at  $x/D = 15$ . The half radius (Fig. 2) is generally larger at  $St = 0.37$  than for  $St = 0$ .

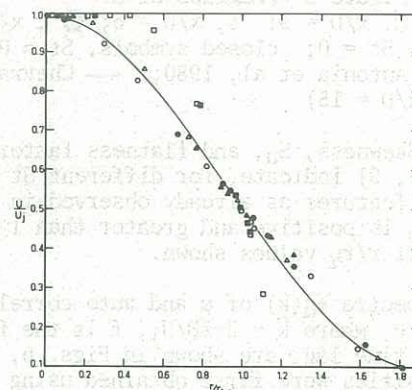


Figure 1 Distribution of mean velocity \*  
\* Symbols same as Figure 3

The relative behaviour of  $r_{1/2}$  at the two values of  $St$  is very similar to that of Zaman (1978) who compared the variation of  $r_{1/2}$  for  $St = 0.85$  ( $R_D = 3.2 \times 10^4$ ) in the same diameter jet with that for the unexcited flow. Zaman found that the slope of  $r_{1/2}$  vs  $x$  was roughly constant after  $x/D = 8$  for both  $St = 0.85$



and 0. Note that  $St = 0.85$  corresponds to the "jet column mode" of excitation, involving stable vortex pairing of vortex rings near  $x/D = 1.75$ , irrespective of whether the initial boundary layer is laminar or turbulent.

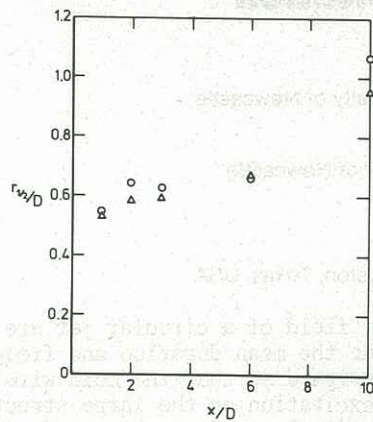


Figure 2 Variation of jet half width with  $x$   
 $\Delta$ ,  $St = 0$ ;  $\circ$ ,  $St = 0.37$

Axial velocity fluctuation intensities are plotted as a function of  $r/r_{1/2}$  in Fig. 3. Also shown are the measurements of Chevray & Tutu at  $x/D = 15$  and of Antonia et al (1980) at  $x/D = 20$  in the same experimental facility. For  $St = 0$  at  $x/D = 2$  and 3 the distributions of  $u'$  with  $r$  are similar but lower than the distributions obtained at  $x/D = 6$  and 10 which are also similar and appear to be approaching self-preservation. For  $St = 0.37$  the  $u'$  distribution is similar as for the unexcited flow at  $x/D = 2$ . The  $u'$  distribution increases with increasing  $x/D$  up to  $x/D = 6$  and then relaxes to a self-preserving profile at  $x/D = 10$ .

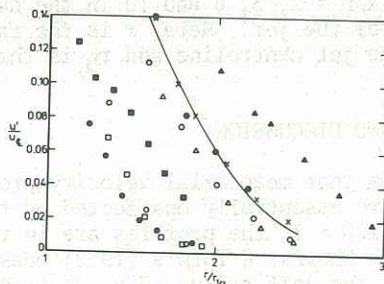


Figure 3 Profiles of  $u'$   
 $\circ$ ,  $x/D = 2$ ;  $\square$ ,  $x/D = 3$ ;  $\Delta$ ,  $x/D = 6$ ;  $\odot$ ,  $x/D = 10$ ;  
open symbols,  $St = 0$ ; closed symbols,  $St = 0.37$ ;  
 $\times$ ,  $x/D = 20$ , Antonia et al, 1980; — Chevray & Tutu, 1978 ( $x/D = 15$ )

Profiles of Skewness,  $S_u$ , and flatness factor,  $F_u$ , of  $u$  (Figs. 4, 5) indicate, for different  $St$  and  $x/D$ , similar features as already observed in the  $u'$  profiles.  $S_u$  is positive and greater than 1 and  $F_u > 3$  for all  $r/r_{1/2}$  values shown.

Normalised spectra  $\phi_u(k)$  of  $u$  and auto correlations  $R_\theta(\tau U_j/D)$  of  $\theta$ , where  $k = 2\pi f D/U_j$ ,  $f$  is the frequency and  $\tau$  the time lag, are shown in Figs. 6, 7. Spectral densities were first obtained using a fast Fourier transform algorithm and the autocorrelations were subsequently generated by doing an inverse Fourier transform. The spectra are normalised so that the integral  $\int_0^\infty \phi_u dk = 1$ . Distributions of  $\phi_u$  indicate the growing importance of the low frequency contribution to  $\phi_u$  with increasing  $x$  and a  $-5/3$  region is evident. With excitation a local peak occurs and the excitation frequency ( $2\pi St$ ), in  $\phi_u$  at  $x/D = 2$  and 3 (contains 26% and 5% respectively of the spectral energy, the area under  $\phi_u$  between the

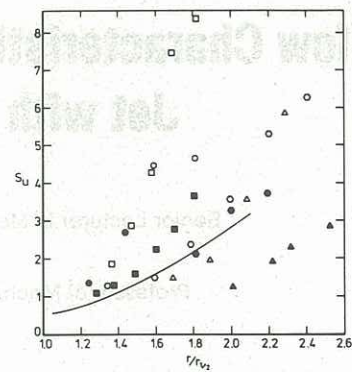


Figure 4 Profiles of  $S_u^*$   
Solid line Chevray & Tutu, 1977 ( $x/D = 15$ )

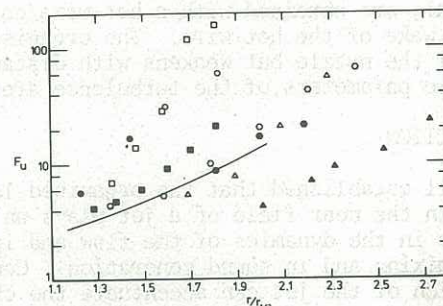


Figure 5 Profiles of  $F_u^*$   
Solid line Chevray & Tutu, 1977 ( $x/D = 15$ )

frequencies neighbouring the excitation frequency). At  $x/D = 2$  a local peak also occurs at the 2nd harmonic (24% of energy) while a weaker bump is observed at the 3rd harmonic of the excitation frequency. At  $x/D = 3$ , a small non-significant deviation occurs in  $\phi_u$  at the 2nd harmonic. At larger values of  $x/D$ , no peaks are evident in the spectra. The reason the turbulent structure at  $x/D = 2$  (as evidenced by  $u'$ ,  $S_u$ ,  $F_u$  distributions) is not affected by excitation is the selective (i.e. narrow band) influence excitation exerted on the spectrum.

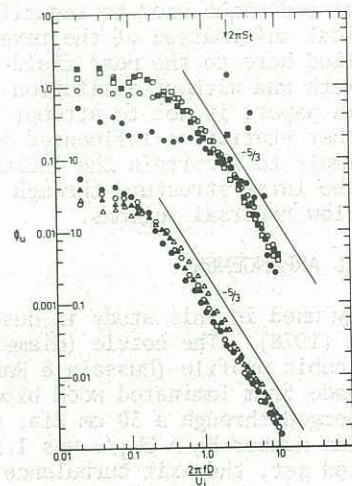


Figure 6 Normalise horizontal velocity spectra \*  
at  $x/D = 2$  and 3,  $r/r_{1/2} \approx 1.6$ ; at  $x/D = 6$  and 10,  
 $r/r_{1/2} \approx 2.3$

Autocorrelations of  $\theta$  indicate for  $x/D = 2$  and 3 a periodic but not sinusoidal (flat troughs and peaked crests), flow reversal for  $St = 0.37$  with the same period as the excitation. Once  $R_\theta$  crosses zero, for  $x/D \geq 6$ , it remains less than 0.05. Crow & Champagne (1971) found from spectra of  $u$  taken along



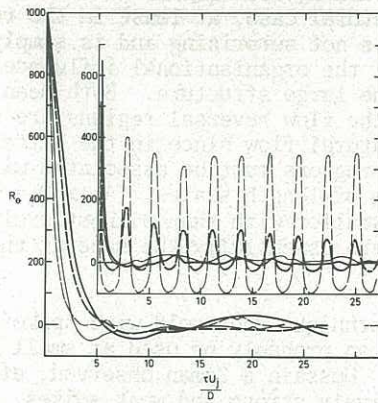


Figure 7 Autocorrelations of temperature. Solid lines,  $St = 0$ ; dashed lines,  $St = 0.37$ ; thin lines,  $x/D = 2$  and  $6$ ; thick lines,  $x/D = 3$  and  $10$ ; same  $r$  as Fig. 6

the centreline of a jet that "large eddies" (vorticity-containing regions of fluid which can be identified as coherent structures in the flow, Yule, 1978), within the first five diameters of the jet exit ( $R_D = 1.1 \times 10^5$ ) can be controlled by application of small excitation levels at the exit plane ( $St = 0.30$ ). No control was possible for  $x > 8D$ . For the present study, effects of the "large eddies" (shown up as spikes in  $\phi_u$  and the periodicity in  $R_0$ ) seem to disappear by  $x/D = 6$ .

The proportion of time  $\alpha$  that the flow reversal occurs (identified by temperature spikes) was obtained by the following detection procedure. A spike occurs whenever the temperature fluctuation  $\theta$  exceeds a selected threshold,  $Th$ , determined by visual scrutiny of temperature traces on the computer display terminal. The sample of  $\theta$  in Fig. 8 (sign of  $\theta$  inverted) clearly shows that the base line is not steady, the relatively low frequency being possibly associated with draughts in the air conditioned room. For this study,  $Th$  was selected by observing the variation of the spike frequency  $F_\alpha$  with  $Th$ . The parameter  $\alpha$  was found not to be as sensitive as  $F_\alpha$  in selecting the threshold voltage. Note that there is no plateau in  $\alpha$  with  $Th$ , a result analogous to the observed lack of independence with  $Th$  of the intermittency factor or fraction of time for which a flow is turbulent. The final choice of  $Th$  corresponded to a relatively sudden change in  $\partial F_\alpha / \partial (Th)$ . In Fig. 8 this occurs at a threshold level of 6.89 volts, the vertical line in the lower plot corresponding to the solid horizontal line in the  $\theta$  trace.

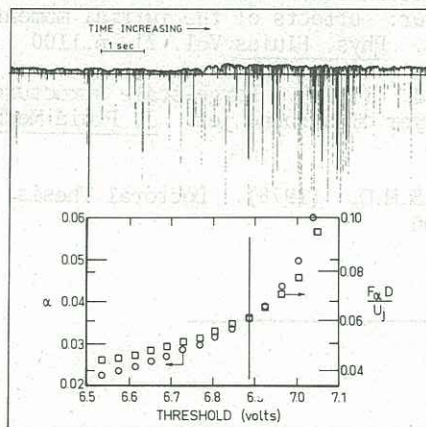


Figure 8 Distributions of  $\alpha$  and  $F_\alpha$  as a function of  $Th$ . Also shown is portion of  $\theta$  trace with  $Th = 6.89$  volts indicated by the solid line.  $\circ$ ,  $\alpha$ ;  $\square$ ,  $F_\alpha$

This technique can only be used to provide relative information, i.e. the absolute values of quantities such as  $\alpha$ ,  $F$  cannot be guaranteed but the relative effect due to variation of  $x$ ,  $r$  and excitation should be reliable.

Distributions of  $\alpha$  and  $F_\alpha$  are shown in Figs. 9, 10. The distributions of  $\alpha$  at different  $x$  either increase with  $r$  or increase at first and then decrease as  $r$  increases. The onset of reverse flow occurs at smaller  $r/r_{1/2}$  for  $x/D = 2$  and  $3$  than for  $x/D = 6$  and  $10$ . There does not appear to be any unique self-preserving curve to which the  $\alpha$  profiles approach at larger  $x/D$  positions. The excited  $\alpha$  profiles at  $x/D = 6$  and  $10$  straddle the  $\alpha$  distribution obtained at  $x/D = 20$  (Antonia et al, 1980). At each station except for  $x/D = 2$ ,  $\alpha$  is larger for  $St = 0$  than  $St = 0.37$ .

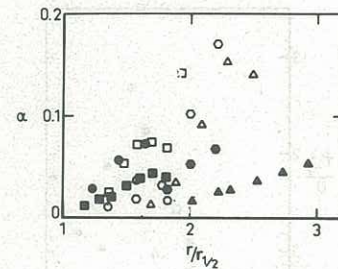


Figure 9 Distribution of  $\alpha$  \*

The frequency of flow reversals for  $St = 0.37$ , slightly less than  $St/2$ , is higher than  $St = 0$  at  $x/D = 2$ . At  $x/D = 3$  the frequency for the two  $St$  is similar, for  $x/D \geq 6$   $F_\alpha$  is greater for  $St = 0$  than  $St = 0.37$ . Generally  $F_\alpha$  first increases and then decreases as  $r/r_{1/2}$  increases. At  $x/D \geq 6$  and  $St = 0.37$ ,  $F_\alpha$  does not change in magnitude and is, to within experimental uncertainty, independent of  $r$ .

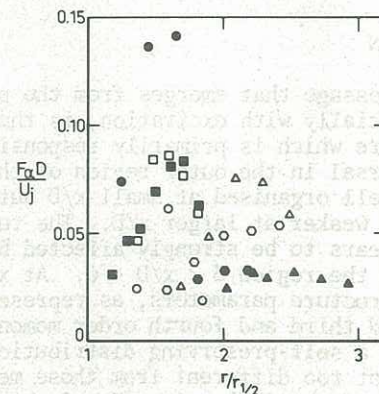


Figure 10 Distribution of  $F_\alpha$  \*

The mean duration  $T$  (Fig. 11a) of flow reversal regions and rms value  $T'$  (Fig. 11b) of the duration of these regions with respect to the mean increase with  $r$  for the range of  $r$  covered by the abscissa. The sampling time interval (normalised by  $U_j$  and  $D$ ) of about 0.3 can be thought to represent a crude estimate of the experimental uncertainty in  $T$  and  $T'$ . The  $T$  and  $T'$  distributions for  $St = 0.37$  are below those for  $St = 0$  at the various  $x$  locations. These profiles for the excited case seem to collapse onto a single curve except at  $x/D = 10$  where the difference between the excited and unexcited values is not great.

The skewness  $S_T$  and flatness  $F_T$  (not shown here) of the duration of flow reversal regions were also obtained. For the unexcited case  $S_T$  and  $F_T$  increase with  $r$ , the rate of increase being much greater at



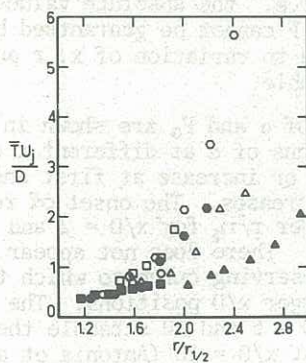


Figure 11a Mean duration of flow reversal,  $T^*$

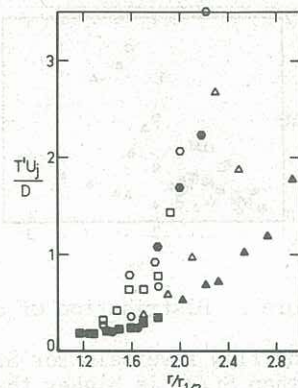


Figure 11b  $T'$

the two stations closer to the jet exit. Of interest are the Gaussian values  $S_T \approx 0$  and  $F_T \approx 3$  obtained at  $x/D = 2, 3$  in the excited jet. Both  $S_T$  and  $F_T$  decrease with increasing  $r$  at  $x/D = 6, 10$  with excitation.

#### 4 CONCLUSION

The overall message that emerges from the present results, especially with excitation, is that the large structure which is primarily responsible for the flow reversal in the outer region of the flow, seems to be well organised at small  $x/D$  but becomes progressively weaker at larger  $x/D$ . The turbulence structure appears to be strongly affected by the excitation in the region  $3 < x/D < 6$ . At  $x/D = 10$ , turbulence structure parameters, as represented by the normalised third and fourth order moments of  $u$  seem to reach a self-preserving distributions (apparently not too different from those measured in the far field of the jet). At  $x/D = 2$ , both the magnitude and frequency of flow reversal regions is large, as evidenced by the  $R_0$  and  $F_\alpha$  results of Figs 9, 10, when excitation is present. In particular, both  $\alpha$  and  $F_\alpha$  are fairly large, the latter being of the same order of magnitude as the forcing frequency. Note that the influence of excitation in this region is so dominant as to be observed in the increase in the mean width of the mixing layer (Fig. 2 for  $x/D$

$= 2$ ). That  $\alpha$  and  $F_\alpha$  are smaller in the excited than in the natural case, at least in the region  $3 < x/D < 6$ , is not surprising and is simply a consequence of the organisational influence excitation has on the large structure. Both mean and rms durations of the flow reversal regions are smaller than in the natural flow since in the latter case, flow reversal regions must be associated with a wider spectrum of length scales. At  $x/D = 10$ ,  $\alpha$  and  $F_\alpha$  are still smaller with than without excitation but  $T$  and  $T'$  are essentially the same at the two values of  $St$ .

The present technique (hot-cold wire spike-catching arrangement) can probably be used at small  $x/D$  ( $< 2$ ) to advantage. Hussain & Zaman observed, at  $x/D = 0.6$ , alternatively strong and weak spikes, associated with consecutive vortices prior to pairing.

#### 5 ACKNOWLEDGEMENTS

A. J. Chambers and R. A. Antonia acknowledge the support of this research by the Australian Research Grants Committee. The authors are indebted to Mr. B. R. Satyaprakash for his assistance during the experiment.

#### 6 REFERENCES

- ANTONIA, R. A., CHAMBERS, A. J. and HUSSAIN A.K.M.F. (1980). Errors in simultaneous measurements of temperature and velocity in the outer part of a heated jet. To appear *Phys. Fluids*
- CHEVRAY, R. and TUTU, N. K. (1977). Conditional measurements in a heated turbulent jet. *Lecture Notes in Physics*, Vol. 76, p.73
- CHEVRAY, R. and TUTU, N. K. (1978). Intermittency and preferential transport of heat in a round jet. *J. Fluid Mech.* Vol. 88, p.133
- CROW, S. and CHAMPAGNE, F. M. (1971). Orderly structure in jet turbulence. *J. Fluid Mech.* Vol. 48, p.547
- HUSSAIN, A.K.M.F. and RAMJEE, V. (1976). Effects of the axisymmetric contraction shape on incompressible turbulent flow. *J. Fluids Engrg.* Vol. 98, p.58
- HUSSAIN, A.K.M.F. and ZAMAN, K.B.M.Q. (1979). Vortex pairing in a circular jet under controlled excitation: part 2. Report FM-2, Department of Mechanical Engineering, University of Houston
- HUSSAIN, A.K.M.F. and ZEDAN, M. F. (1978). Effects of the initial conditions on the axisymmetric free shear layer: effects of the initial momentum thickness. *Phys. Fluids* Vol. 21, p.1100
- YULE, A. J. (1978). Large-scale structure in the mixing layer of a round jet. *J. Fluid Mech.* Vol. 89, p.413
- ZAMAN, K.B.M.Q. (1978). Doctoral Thesis, University of Houston